**Mathematical structural descriptors and mutagenicity assessment: A study with congeneric and diverse data sets**

Subhabrata Majumdar, Subhash C. Basak, Claudiu N. Lungu, Mircea V. Diudea, Gregory D. Grunwald

Abstract: Quantitative activity assessment of chemical compounds plays a central role in drug discovery as it saves a substantial amount of resources. To this end, high-performance computing has enabled researchers and practitioners to leverage hundreds, or even thousands, of synthetic descriptors for activity prediction of candidate compounds. In this paper, we evaluate the utility of two large groups of chemical descriptors in such predictive modelling, as well as chemical structure discovery, through empirical analysis. We use a suite of commercially available and in-house softwares to calculate these descriptors for two sets of compounds- a homogeneous set of 95 amines, and a diverse set of 508 chemicals. Using calculated descriptors, we model the mutagenic activity of these compounds using a number of methods from the statistics and machine learning literature, and use robust principal component analysis to investigate the low-dimensional subspaces that characterize these chemicals. Our results suggest that combining different sets of descriptors is likely to result in a better predictive model- but that depends on the compounds being modeled and the modelling technique being used.

Keywords: Chemical descriptors; variable selection; dimension reduction; machine learning; mutagenicity; QSAR

**1. INTRODUCTION**

Hazard assessment of chemicals is often carried out in data poor situations [1]. The Toxic Substances Control Act (TSCA) Inventory, maintained by the United States Environmental Protection Agency (USEPA), currently has about 85,000 entries [2]. A large fraction of these chemicals has very little or no data needed for their hazard estimation [3]. The assessment of chemical mutagenicity is important both for environmental protection and drug discovery. Identification of potential mutagenicity for industrial chemicals and environmental pollutants is prerequisite to the protection of human and ecological health. For drug discovery, early mutagenicity detection for drug candidates can help in the effective allocation of resources in drug design protocol which costs on the average over US $2 billion [4].

Laboratory testing of mutagenicity for all possible candidate chemicals, can be very expensive. Therefore, assessment of potential mutagenicity of chemicals from Quantitative Structure-Activity Relationship (QSAR) models has been accepted for evaluation of chemicals in lieu of experimental mutagenicity data [5]. Such models carry out property/ bioactivity/ toxicity assessment *in silico,* i.e. without actually performing the experiments, and using quantitative modelling techniques instead that predict roperties of compounds using molecular descriptors. In the early stages of QSAR during the middle of the 20th century, the effectiveness of such approaches was limited by the handful of descriptors that could be calculated using the limited computational resources available. This situation has drastically changed in the past two or three decades. High-performance computing has enabled researchers to calculate hundreds or even thousands of descriptors using various softwares [6, 7][8,9,10,11] in a reasonable amount of time, thus generating a vast amount of information to potentially build effective models for chemical activity prediction. For this reason, development, computation and usage of chemical descriptors has a central role in the present landscape of QSAR research.

In this paper, we consider two approaches towards QSAR descriptor calculation and present an evaluation of their utility. The first set of descriptors [8, 9, 10, 11] consist of those developed and used by Basak and coworkers over the past decades towards effective QSAR model formulation [12, 13, 7, 14, 15]. The second descriptor set has been developed by Diudea and coworkers using Schrodinger and in-house software TopoCluj [16, 17, 18]. Examples of their effectiveness in mapping the chemical activity landscape include [19, 20]. Keeping the above in mind, the goal of this paper is two-fold: 1) Present a comparison of the two predictor sets (separately and combined) for the mutagenicity assessment of two data sets, viz., a homogeneous set of 95 aromatic and heteroaromatic amines and a structurally diverse set of 508 chemicals using a battery of various statistical and machine learning approaches, and 2) use robust principal component analysis to explore how the combined set of descriptors map the underlying low-dimensional subspace of chemical properties.

The rest of the paper is organized as follows. Section 2 presents the details of our methodology- data, descriptors, and techniques used for model building and validation. In section 3, we present and elaborate on the findings from our analysis. We conclude the paper with a discussion in section 4.

**2. MATERIALS AND METHODS**

**2.1. Data**

The two datasets used in this paper represent two different use cases that practitioners are likely to enter while doing QSAR analysis. The first data consists of the mutagenic activities of 95 congeneric amines on bacterial samples from the TA98 *S. typhimurium* strain [21]. The response variable, measured as the log number of revertants per nmol when a chemical compound is applied to the *S. typhimurium* test cultures, were studied in the original study by Debnath *et al* [21]*.* While the compounds in this dataset are very similar to each other in chemical structure, our second dataset consists of data on 508 chemical compounds from several different chemical classes. **Table 1** summarizes this classification of the chemical compounds (note that a compound can belong to two or more classes). Collected from the CRC Handbook of Identified Carcinogens and Non-carcinogens [22], the response variable in this dataset is the 0/1 Ames mutagenicity status of the chemical compounds. In total the data contains 256 mutagens and 252 non-mutagens. For each set of compounds, we calculated their corresponding descriptors sets using two sets of softwares, previously used by Basak *et al* [13, 12, 14] and Diudea *et al* [23].

*Table 1: Chemical classes of samples in the 508 compound diverse dataset*

|  |  |
| --- | --- |
| Chemical class | Number of compounds |
| Aliphatic alkanes, alkenes, alkynes | 124 |
| Monocyclic compounds | 260 |
| Monocyclic carbocycles | 186 |
| Monocyclic heterocycles | 74 |
| Polycyclic compounds | 192 |
| Polycyclic carbocycles | 119 |
| Polycyclic heterocycles | 73 |
| Nitro compounds | 47 |
| Nitroso compounds | 30 |
| Alkyl halides | 55 |
| Alcohols, thiols | 93 |
| Ethers, sulfides | 38 |
| Ketones, ketenes, imines, quinones | 39 |
| Carboxylic acids, peroxy acids | 34 |
| Esters, lactones | 34 |
| Amides, imides, lactams | 36 |
| Carbamates, ureas, thioureas, guanidines | 41 |
| Amines, hydroxylamines | 143 |
| Hydrazines, hydrazides, hydrazones, traizines | 55 |
| Oxygenated sulfur and phosphorus | 53 |
| Epoxides, peroxides, aziridines | 25 |

**2.2. Descriptors**

For this study we have used two collections of molecular descriptors. One set of descriptors, used frequently by the Cluj team of Diudea and collaborators, were calculated by the programs Schrodinger [16] and TopoCluj [17]. More detailed references about these descriptors are given in Supplementary Tables 1 and 4. For the 95 and 508 data sets, 185 and 201 descriptors were calculated by Diudea *et al*.

The second set of molecular descriptors, used frequently by Basak *et al*, were calculated by the software POLLY [8], MolConnZ [24], Triplet [11], and MOPAC [9]. For the 95 and 508 chemical sets, 275 and 307 descriptors were calculated for this paper by these software. Among them, 18 descriptors were common with the Cluj descriptors for the 95 amines data, while for the 508 compound diverse dataset there were 22 common descriptors. Thus the number of descriptors in the union of these two sets are 442 and 486, respectively.

**2.3. Statistical and machine learning methods**

We use three types of methods to build our predictive models.

*2.3.1. Dimension reduction*

The hundreds of descriptors generally used in chemometric analysis generally have a high degree of correlation among them [25]. For this reason, dimension reduction techniques, such as Principal Component Analysis (PCA) or Partial Least Squares (PLS) have seen widespread use in QSAR model building [26, 27, 28]. In this paper, we build predictive models using the following two dimension reduction methods:

*Principal Component Regression (PCR)*: We transform descriptor matrix **X**, we transform it by multiplying with a principal component loading matrix:

Where the number of columns in **Γ** denote the minimum number of principal components (PCs) that explain 95% of the total underlying variation. We follow the analysis of Majumdar and Basak [28] and apply a robust PCA procedure [29] to obtain the PC loadings. Following this, we use the transformed data matrix as the matrix of predictors in linear and logistic regression models to predict activities in the 95 and 508 compound datasets, respectively.

*Partial Least Squares (PLS)*: Another popular method in QSAR literature, PLS uses latent variables to model the correlation between predictors and the response variables. Mainly used to build models used in prediction purposes, PLS obtains a sequence of linear regression coefficients by successively regressing orthogonal components in the data matrix on those in the response vector.

*2.3.2. Variable selection*

Since the datasets we are dealing with are inherently high-dimensional (i.e. large number of predictors that can potentially be more than the number of samples), we use sparse regression methods for variable selection.

*Least Absolute Shrinkage and Selection Operator (LASSO)*: In a linear or generalized linear model, the lasso method [ref] obtains *sparse* estimates of the coefficient estimates by setting some entries to exactly zero. In the QSAR context, this means some predictors will have zero effect on the response variable. Thus, the lasso method is able to perform simultaneous variable selection and model building.

*Smoothly Clipped Absolute Deviation penalty (SCAD)*: Proposed by Fan and Li [30], SCAD is another penalization method that selects sparser models than lasso, i.e. models where more entries in the coefficient vector are set at 0, without compromising on the predictive capability of the model.

*2.3.3. Machine learning*

Our goal in this paper is to assess and compare the predictive capabilities of different descriptor sets. Machine learning methods are known to produce models with high predictive performance, even though interpreting such ‘black box’ models is often difficult [31]. For this reason, we use the following two methods in our study.

*Random Forest (RF)*: This method trains multiple decision trees on a dataset, each based on a randomly selected subset of total features. The final prediction in a regression problem is taken as the average of individual predictions from all the trees, while in classification problem the final class prediction is done by majority voting. Previous examples of the use of RF models in QSAR include [32, 33, 34].

*Gradient Boosting Machine (GBM)*: Gradient boosting attempts to fit the data using multiple ‘weak learners’, which are simple models that work slightly better than random guessing. At first a weak learner is trained on the data, residuals are obtained from that model and those are again fit using weak learners. Boosting methods have proven to be very useful in predictive model building since their proposal. Examples of boosting in the QSAR scenario include [35, 36].

**2.4. Validation**

We use a ‘two-deep’ multi-split cross validation scheme to evaluate our predictive methods. Multi-split means we consider multiple random train-test splits of the data, build a model on the train partition, evaluate them on the test partition, and compare different methods using the average values of a metric (e.g. Root Mean Squared Error, Area Under Curve etc.) across all such test sets. This has been referred in the QSAR literature as Monte-Carlo Cross Validation [37], and ensures that the true underlying components in a model (e.g. important predictors or principal components) are more and more likely to be recovered accurately as sample size increases [37, 38]. The phrase ‘two-deep’ means we repeat the dimension reduction/ tuning parameter selection steps of the method being implemented. This ensures that information from the test samples are not used while training the model, and gives a more accurate picture of the predictive capability of the technique being analyzed [39, 7, 40, 41].

**3. RESULTS**

In this section, we state and discuss the outputs from our analysis. Section 3.1 is concerned about the predictive models and the comparison of outputs across different methods and predictor sets, while in Section 3.2 we list the top principal components for evaluating the effects of the new Cluj descriptors with respect to previous findings on the same datasets. All data analyses were done using the statistical software R v3.3.2 [42].

**3.1. Output of predictive models**

*Table 2: Average and standard deviations (in brackets) of Area Under Curve (AUC) for different methods applied on the 508 compounds heterogeneous dataset*

|  |  |  |  |
| --- | --- | --- | --- |
| **Method** | **Descriptor set used** | | |
| **Combined** | **Basak lab** | **Diudea lab** |
| **PCR** | 0.59 (0.055) | **0.78 (0.038)** | 0.58 (0.057) |
| **PLS** | **0.86 (0.035)** | 0.85 (0.033) | 0.79 (0.038) |
| **Lasso** | 0.72 (0.048) | **0.75 (0.045)** | 0.63 (0.06) |
| **SCAD** | 0.57 (0.061) | 0.58 (0.059) | **0.62 (0.063)** |
| **RF** | **0.81 (0.036)** | 0.80 (0.042) | 0.79 (0.040) |
| **GBM** | 0.80 (0.04) | **0.82 (0.04)** | 0.75 (0.042) |

It is evident from the results in Table 2 above that the PLS method with the combined set of descriptors gives the best predictive model (AUC = 0.86) while the model based on Basak group index only is also close second (AUC = 0.85).

*Table 3: Median and mean absolute deviations (in brackets) of Mean Square Prediction Error (MSPE) for different methods applied on the 95 amines dataset*

|  |  |  |  |
| --- | --- | --- | --- |
| **Method** | **Descriptor set used** | | |
| **Combined** | **Basak lab** | **Diudea lab** |
| **PCR** | **29.11 (13.79)** | 57.08 (93.829) | 76.02 (24.72) |
| **PLS** | **18.86 (6.03)** | 19.86 (7.464) | 75.70 (24.689) |
| **Lasso** | **26.85 (9.049)** | 28.72 (8.825) | 72.75 (17.998) |
| **SCAD** | **25.81 (8.962)** | 31.77 (21.442) | 74.94 (18.322) |
| **RF** | **17.25 (6.498)** | 18.98 (6.587) | 84.59 (21.735) |
| **GBM** | **14.79 (5.836)** | 18.03 (6.296) | 74.78 (17.426) |

For the congeneric set of 95 aromatic and heteroaromatic amines, the PLS, RF and GBM methods yield the best predictive models when the combined sets of descriptors were used. Results derived the Basak group indices only came out as close second ones.

Methods that depend directly on sparse linear combinations of predictors: Lasso, SCAD do not perform well in either case. This means there is high degree of nonlinearity among the relationship between the responses and predictors, and activities of compounds are more dependent on lower-dimensional subspaces in the predictor space than individual predictors. These subspaces are often predictive of the response, as corroborated by the good performance of PLS for both the datasets. PLS has the best performance among all methods on the combined set of predictors in the 95 amines data, and performs competitively in the more diverse 508 compounds dataset.

Interestingly, for the 508 compounds dataset, more predictors do not always equate to better prediction. A reason for this can be the fact that this dataset is composed of chemical compounds from diverse classes. In comparison, the homogeneous 95 compound dataset always gives better prediction with the combined set of predictors than either group of predictors alone.

**3.2. Principal Component Analysis of descriptor sets**

The results obtained using the robust PCA procedure are presented in Tables 4 and 5 and the below discussion. Interestingly, even though the Diudea set of descriptors do not perform well in prediction by themselves, they come up almost completely as the ones with top loadings in the robust PCA results.

*Table 4: Top PC loadings of the 95 amines data*

|  |  |  |  |
| --- | --- | --- | --- |
| **PC1 (12.5%)** | **PC2 (10.3%)** | **PC3 (7.1%)** | **PC4 (6.9%)** |
| E\_ele (0.69) | E\_ele (-0.42) | E\_ele (-0.35) | E\_vdw (-0.73) |
| vsurf\_EWmin1 (-0.43) | vsurf\_EWmin1 (-0.27) | vsurf\_EWmin1 (-0.33) | E\_nb (-0.48) |
| vsurf\_EWmin2 (-0.4) | vsurf\_EWmin2 (-0.25) | E\_vdw (-0.31) | E\_ele (0.34) |
| vsurf\_EWmin3 (-0.3) | vsurf\_DW13 (-0.21) | vsurf\_EWmin2 (-0.31) | vsurf\_EWmin1 (0.19) |
| vsurf\_DW13 (-0.17) | vsurf\_EWmin3 (-0.18) | E\_nb (-0.27) | vsurf\_EWmin2 (0.18) |
| E\_nb (0.11) | E\_nb (-0.17) | vsurf\_EWmin3 (-0.23) | vsurf\_DW13 (-0.14) |
| vsurf\_HB6 (0.08) | E\_vdw (-0.17) | vsurf\_DW13 (0.21) | vsurf\_EWmin3 (0.13) |
| vsurf\_W6 (0.08) | DN2Z2 (0.16) | **DN2Z2 (-0.16)** | GCUT\_SlogP\_0 (0.06) |
| vsurf\_HL2 (0.06) | SlogP\_VSA9 (0.13) | GCUT\_SMR\_0 (–0.11) | GCUT\_SMR\_0 (0.06) |
| vsurf\_CW6 (0.06) | **ASZ2 (0.12)** | **ASZ2 (-0.1)** | **DN2Z2 (0.04)** |

**Bold** = Triplet descriptors

For the 95 amines data set, first four PCs explained 36.8% of the variance in the data, and it needs 28 PCs to explain 90% of the total variance. These PCs represent important features of chemical graph. Since PCs are orthogonal to each other, higher order PCs do not contain characteristics other than those encoded in the first four PCs. Most of the toxic properties of these 95 compounds are related to their solubility surface and membrane permeability capacity. The energetic variable E\_ele has very high loadings across all PCs (Highest for PC1 to 3, third highest for PC4), advising that the activity of 95 amines is possibly guided by an energetic dependent process, i.e. interaction with a potential target. These loadings are positive for PC1 and PC4, while negative for the other two: which is justified by the dynamic nature of the interaction. These values reflect distinct structural states, possibly conformational changes in compounds by virtue of interaction with a certain target.

*Table 5: Top PC loadings of the 508 compounds data*

|  |  |  |  |
| --- | --- | --- | --- |
| **PC1 (15%)** | **PC2 (14.1%)** | **PC3 (12%)** | **PC4 (9.3%)** |
| E\_tor (0.96) | vsurf\_DW23 (0.95) | density (-0.93) | GCUT\_SlogP\_0 (0.96) |
| vsurf\_DW23 (-0.25) | E\_tor (0.23) | GCUT\_SlogP\_0 (-0.19) | density (-0.19) |
| GCUT\_SlogP\_0 (0.06) | GCUT\_SlogP\_0 (0.15) | vsurf\_ID2 (0.12) | vsurf\_DW23 (-0.14) |
| vsurf\_ID3 (-0.04) | density (-0.07) | vsurf\_ID3 (0.12) | E\_tor (-0.09) |
| vsurf\_ID4 (-0.04) | vsurf\_ID2 (-0.06) | vsurf\_ID4 (0.11) | vsurf\_CP (0.05) |
| vsurf\_ID2 (-0.04) | vsurf\_ID1 (-0.05) | vsurf\_ID1 (0.1) | vsurf\_ID2 (0.04) |
| vsurf\_ID6 (-0.03) | vsurf\_ID3 (-0.05) | vsurf\_IW1 (0.1) | vsurf\_ID4 (0.02) |
| vsurf\_ID1 (-0.03) | vsurf\_ID4 (-0.04) | vsurf\_ID5 (0.09) | vsurf\_ID3 (0.02) |
| vsurf\_ID5 (-0.03) | vsurf\_CW4 (-0.04) | BCUT\_SMR\_2 (-0.09) | vsurf\_ID1 (0.02) |
| vsurf\_ID7 (-0.03) | vsurf\_ID6 (-0.03) | vsurf\_ID6 (0.07) | vsurf\_ID7 (0.02) |

For the 508 structurally diverse set, first four PCs explained 50.3% of the variance in data, and 12 PCs were needed to explain 90% of total variance. Loadings in case of this compounds are high with respect to intrinsic physico-chemical properties. The top 4 PCs have highest loadings for the following relevant variables: E\_tor (0.96), vsurf\_DW23 (0.95), density (-0.93), GCUT\_SlogP\_0 (0.96), which are part of the so-called ‘absorption, distribution, metabolism, and excretion’ (ADME) features.

**4. Discussion**

In this paper we explored the utility of two large sets of chemical descriptors (separately and combined) using a case study on two sets of chemical compounds. Our findings highlight the fact that a higher number of descriptors is often beneficial for predictive model building- but that is contingent on the specific set of compounds being modeled, as well as the use of proper modelling and validation techniques.

**5. CONFLICT OF INTEREST**

We confirm that there is no conflict of interest on the content of this paper.

**6. ACKNOWLEDGEMENTS**

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**7. SUPPLEMENTARY MATERIAL**

Supplementary material (Supplementary tables 1-4) is available on the publisher’s web site along with the published article.

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